ACHARYA NAGARJUNA UNIVERSITY

A State Government University, Accredited with "A" Grade by NAAC Nagarjuna Nagar - 522 510, Guntur, Andhra Pradesh, India.



M.Sc. STATISTICS



2022 - 2023 onwards

UNIVERSITY COLLEGE OF SCIENCES

PROGRAM CODE:

ANUCS17





ACHARYA NAGARJUNA UNIVERSITY (ANU)

- A Brief Profile

Acharya Nagarjuna University, a State University established in 1976, has been constantly striving towards achieving progress and expansion during its existence for over four decades, in terms of introducing new courses in the University Colleges, affiliated colleges and professional colleges. Spread over 300 acres of land on the National High Way (NH-16) between Vijayawada and Guntur of Andhra Pradesh, the University is one of the front ranking and fastest expanding Universities in the state of Andhra Pradesh. The University was inaugurated on 11th September, 1976 by the then President of India, Sri Fakruddin Ali Ahmed and celebrated its Silver Jubilee in 2001. The National Assessment and Accreditation Council (NAAC) awarded "A" grade to Acharya Nagarjuna University and also has achieved 108 International ranks, 39 National ranks UI Green Metrics rankings and many more It is named after Acharya Nagarjuna - one of the most brilliant preceptors and philosophers, whose depth of thought, clarity of perception and spiritual insight were such that even after centuries, he is a source of inspiration to a vast number of people in many countries. The University is fortunate to be situated on the very soil where he was born and lived, a soil made more sacred by the aspiration for light and a state of whole someness by generations of students. With campus student strength of over 5000, the University offers instruction for higher learning in 68 UG & PG programs and guidance for the award of M.Phil. and Ph.D. in 48 disciplines spread over six campus colleges and one PG campus at Ongole. It also offers 160 UG programs in 440 affiliated colleges in the regions of Guntur and Prakasam Districts. It has a Centre for Distance Education offering 87 UG & PG programs. Characterized by its heterogeneous students and faculty hailing from different parts of the state and the country, the University provides most hospitable environment for pursuing Higher Learning and Research. Its aim is to remain connected academically at the forefront of all higher educational institutions. The University provides an excellent infrastructure and on- Campus facilities such as University Library with over one lakh books & 350 journals; Computer Centre; University Scientific Instrumentation Centre; Central Research Laboratory with Ultra-modern Equipment; Well-equipped Departmental Laboratories; Career Guidance and Placement Cell; Health Centre; Sports Facilities with Indoor & Outdoor Stadiums and Multipurpose Gym; Sports Hostel; Separate hostels for Boys, Girls, Research Scholars and International Students; Pariksha Bhavan (Examinations Building); Computers to all faculty members; Wi-Fi connectivity to all Departments and Hostels; Canteen, Student Centre & Fast-food Centre; Faculty Club; Dr. H.H. Deichmann & Dr. S.John David Auditorium cum Seminar Hall; Post office; Telecom Centre; State Bank of India; Andhra Bank; Energy Park; Silver Jubilee Park; Fish ponds; internet center; xerox center; cooperative stores; Water harvesting structures.



ACHARYA NAGARJUNA UNIVERSITY

VISION

To generate sources of knowledge that dispels ignorance and establish truth through teaching, learning and research.

MISSION

To promote a bank of human talent in diversified faculties – Commerce & Management Studies, Education, Engineering & Technology, Humanities, Law, Natural Sciences, Pharmacy, Physical Education & Sports Sciences, Physical Sciences and Social Sciences that would become an investment for a prosperous society.

OBJECTIVES

- ▲ To inspire and encourage all who would seek knowledge through higher education and research.
- ▲ To provide quality instruction and research for the advancement of science and technology.
- ▲ To promote teaching and research studies in disciplines of societal relevance.
- ▲ To bridge the gap between theory and practice of the principles of higher education.
- ▲ To develop human talent necessary for the industry.
- ▲ To open up avenues of higher education and research through non-formal means.
- ▲ To invite and implement collaborations with other institutes of higher learning on a continuous basis for mutual academic progress.
- ▲ To motivate and orient each academic department/centre to strive for and to sustain advanced levels of teaching and research so that the university emerges as an ideal institute of higher learning.
- ▲ To focus specially on the studies involving rural economy, justifying its existence in the rural setting.



ACHARYA NAGARJUNA UNIVERSITY UNIVERSITY COLLEGE OF SCIENCES

VISION OF THE COLLEGE:

University College of Sciences envisages to be a good team of people with scientific temperament, research bent and a flair for Teaching & Learning for the betterment of the Community, Society, State and the Country at large.

MISSION OF THE COLLEGE:

The College intends to incubate and nurture the Leaders, Mentors, Educators and researchers who can transform the country and contribute to advances in science while addressing the challenges faced by the society for the betterment of human life.





ACHARYA NAGARJUNA UNIVERSITY UNIVERSITY COLLEGE OF SCIENCES DEPARTMENT OF STATISTICS

VISION OF THE DEPARTMENT:

To develop committed competent, efficient and professionally trained statisticians of quality education and to bring out potentialities in the students.

MISSION OF THE DEPARTMENT:

To prepare the statisticians with good values, to import wisdom that will give an opportunity to enhance their ability to apply statistics in diversified areas and to encourage students to promote their expertise in statistical skills such as statistical data analysis using software's (R/SPSS/Minitab/Python) and to take leadership role in the development of the country.



ACHARYA NAGARJUNA UNIVERSITY UNIVERSITY COLLEGE OF SCIENCES DEPARTMENT OF STATISTICS M.Sc. STATISTICS

PROGRAMME OUTCOMES AND PROGRAMME SPECIFIC OUTCOMES:

The duration of the course of instruction for M.Sc. Statistics programme shall be of two years (Four Semesters).There will be Four Theory Papers and Two Practicals in each semester. In addition of theory and practicals, students will have to submit a project work report in M.Sc. second year. The detailed scheme of examinations for M.Sc. Statistics programme is as follows:-

PROGRAM OUTCOMES (PO's):

Number	Outcomes
PO-1	Recognize and think critically towards the subject Statistics curricula with sound
	knowledge and theoretical skills by questioning and plausible explanations.
PO-2	Nurturing the curious minds towards translation and application of statistical knowledge to find solution to real-world problems.
PO-3	Preparing the next generation statistician ready for scientific decision-making, aided with advanced statistical software translating into sharp and extensive analytics, pertinent to various domains.
PO-4	Support critical thinking for data driven solution with advanced methodologies and applicable statistical software packages like R, SPSS, MINITAB etc for scientific decision-making.
PO-5	Learn specific sets of disciplinary or multidisciplinary skills and advanced techniques and apply them for betterment of mankind.
PO-6	Train non statisticians to handle Statistical and data analytics with Career opportunities in public and private sectors such as Government, Insurance, Banking, Finance, Automobile, Information Technology, Pharma and many other sectors that will entail market research, forecasting and predictive analysis.
PO-7	Project management of finance in collaboration with various firms by data science techniques.

Number	Outcomes
PSO-1	Acquire sound knowledge in theoretical and practical aspects of Statistics.
PSO-2	Achieve skills to handle the real life problems through practicals and project work using suitable Statistical tools and software such as SPSS, MINI TAB and R software.
PSO-3	Acquire the ability to formulate suitable statistical models and their fitting to real life Data.
PSO-4	Enhance skills to carry out innovative research in the subjects Statistics, Mathematics and Operations Research.
PSO-5	Capability to use appropriate statistical skills in interdisciplinary areas such as finance, health, agriculture, government, business, industry, telecommunication, bio-statistics and Time-series.
PSO-6	Develop confidence to acquire new statistical knowledge and expertise for a better career in statistics and also to compete in civil services, Indian statistical services and other allied services.

PROGRAM SPECIFIC OUTCOMES (PSO's):





ACHARYA NAGARJUNA UNIVERSITY UNIVERSITY COLLEGE OF SCIENCES DEPARTMENT OF STATISTICS

M.Sc. STATISTICS

TWO YEAR M.Sc. COURSE IN STATISTICS COURSE STRUCTURE AND EXAMINATION SCHEME

(with effect from 2022-2023 admitted batch of students)

S. No.	Components of Study	Course Code	Title of the Course	Contact Hours / week	No. of Credits	Internal Assessment Marks	Semester End Examination Marks	Total Marks
1	Core	S 1.1 (22)	Probability Theory and Distributions	65	4	30	70	100
2		S 1.2 (22)	Statistical Computing Using R	6	4	30	70	100
3	Compulsory Foundation	S 1.3 (22)	Estimation	6	4	30	70	100
4	*Elective Foundation	S 1.4 (a) (22) S 1.4 (b) (22)	a) Sampling Theoryb) Linear Algebra	6	4	30	70	100
5	Practical-I	S 1.5 (22)	Papers on S 1.1 (22) & S 1.2 (22) - Statistical Software Practical using R	6	4	30	70	100
6	Practical-II	S 1.6 (22)	Papers on S 1.3 (22) & S 1.4 (22)	6	4	30	70	100
		TOT	AL	36	24	180	420	600

SEMESTER-I

* The student shall choose <u>ONE PAPER</u> from Elective Foundation

S. No.	Components of Study	Course Code	Title of the Course	Contact Hours / week	No. of Credits	Internal Assessment Marks	Semester End Examination Marks	Total Marks
1	Core	S 2.1 (22)	Multivariate Analysis	6	4	30	70	100
2		S 2.2 (22)	Testing of Hypothesis	6	4	30	70	100
3	Compulsory	S 2.3 (22)	Theory of Linear Estimation	6	4	30	70	100
	Foundation		and Analysis of Variance					
4	*Elective	S 2.4 (a) (22)	a) Stochastic Processes	6	4	30	70	100
	Foundation	S 2.4 (b) (22)	b) Linear Models and Applied Regression Analysis					
5	Practical-I	S 2.5 (22)	Papers on S 2.1 (22) & S 2.2 (22) - Statistical Software Practical using SPSS and R	6,111	4	30	70	100
6	Practical-II	S 2.6 (22)	Papers on S 2.3 (22) & S 2.4 (22)	6	4	30	70	100
7	Skill Development Course		MOOCS Course	ARJU	4			
		TOTAL		36	28	180	420	600

SEMESTER-II

* The student shall choose <u>ONE PAPER</u> from Elective Foundation



SEMESTER-III

S. No.	Components of Study	Course Code	Title of the Course	Contact Hours / week	No. of Credits	Internal Assessment Marks	Semester End Examination Marks	Total Marks
1	Core	S 3.1 (22)	Design of Experiments	6	4	30	70	100
2		S 3.2 (22)	Statistical Quality Control	6	4	30	70	100
3	Elective - I	S 3.3 (a) (22)	a) Actuarial Statistics	6	4	30	70	100
		S 3.3 (b) (22)	b) Time Series Analysis					
4	Elective - II	S 3.4 (a) (22)	a) Reliability – I	6	4	30	70	100
		S 3.4 (b) (22)	b) Biostatistics					
5	Practical-I	S 3.5 (22)	Papers on S 3.1 (22) & S 3.2 (22) - Statistical Software Practical using SPSS and R	6	4	30	70	100
6	Practical-II	S 3.6 (22)	Papers on S 3.3 (22) & S 3.4 (22)	6	4	30	70	100
7	Skill Enhanced Course		MOOCS Course	AGAR	4			
		ΤΟ	TAL	36	28	180	420	600

*The student shall choose ONE PAPER from each of Elective-I and Elective-II



S. No.	Components of Study	Course Code	Title of the Course	Contact Hours / week	No. of Credits	Internal Assessment Marks	Semester End Examination Marks	Total Marks
1	Core	S 4.1 (22)	Econometrics	6	4	30	70	100
2		S 4.2 (22)	Acceptance Sampling Plans	6	4	30	70	100
3	Elective - I	S 4.3 (a) (22)	a) Operations Research	6	4	30	70	100
		S 4.3 (b) (22)	b) Machine Learning Using Python					
4	Elective - II	S 4.4 (a) (22)	a) Reliability – II	6	4	30	70	100
		S 4.4 (b) (22)	b) Knowledge Discovery and Data Mining		2			
5	Practical-I	S 4.5 (22)	Papers on S 4.1 (22) & S 4.2 (22) - Statistical Software Practical using SPSS and R	6	4	30	70	100
6	Practical-II	S 4.6 (22)	Papers on S 4.3 (22) & S 4.4 (22)	6	4	30	70	100
7	Project Wor	k			4		100	100
		TO	DTAL	36	28	180	420	700
			TOTAL SEMESTERS: I + II + III -	IV/S				2500

The student shall choose <u>ONE PAPER</u> from each of Elective-I and Elective-II





ACHARYA NAGARJUNA UNIVERSITY UNIVERSITY COLLEGE OF SCIENCES DEPARTMENT OF STATISTICS M.Sc. STATISTICS

SEMESTER-I

S 1.1 (22) :: PROBABILITY THEORY AND DISTRIBUTIONS

Credits: 4

COURSE OBJECTIVES:

- CO1: To explore the students to study the fundamental concepts of probability and probability measures.
- CO2: To get expertise in analyzing the random phenomenon through convergence of random variable.
- CO3: To be able to understand different types of inequalities associated with mathematical expectations.
- CO4: To able to understand the concept of law of large numbers and their applications.
- CO5: To get expertise in understanding the advanced probability distributions and utilizing them to model the random phenomenon.
- CO6: To understand Discrete and Continuous distributions and its applications in data analysis.
- CO7: To acquainted with distributions of order statistics of various random variable and their applications.

LEARNING OUTCOMES:

After successful completion of this course, student will be able to:

- LO1: Aanalyse datasets with sound probability theory for scientific knowledge discovery.
- LO2: Understand and analyse random phenomenon of different events.
- LO3: Model stochastic nature through probability distributions.
- LO4: Apply probability and distribution theory in solving practical problems.
- LO5: Fit appropriate distribution for the given grouped data.

Unit I:

Classes of sets, fields, σ fields, minimal σ fields, sequence of sets, limit supremum and limit infimum of sequence of sets, measure, probability measure, properties of measure, axiomatic definition of probability, continuity theorem of probability, conditional probability, statistical independence of events, probability on finite sample spaces, geometrical probability.

Unit -II

Measurable functions, notation of random variable, distribution function, properties of distribution, vector of random variables, statistical independence, concepts of joint, marginal and conditional distributions, mathematical expectation, conditional expectation, characteristic function, its properties. Inversion formula, characteristic functions and moments. Moments inequalities-Markov, Schwartz, Jensen, Holder, Minkowski, Kolmogrove's, Hajek-Renyi.

Unit -III

Convergence of sequence of random variables-Type of convergence-in probability, almost sure, in mean square, in law- their interrelations. Law of large numbers-weak laws: Chebychevs's form of W.L.L.N., Necessary and Sufficient Condition of W.L.L.N. Kintchines form of W.L.L.N., Kolmogrove's S.L.LN for i.i.d. random variables.

Unit -IV

Discrete distributions - Compound Binomial, Compound Poisson, multinomial, truncated Binomial, truncated Poisson distributions and their properties. Continuous distributions-Laplace, Weibull, Logistic and Pareto distributions and their properties.

UNIT-V

Order statistics- distribution function, probability density function (p.d.f.) of single order statistic, joint p.d.f. of order statistics. Distribution of range with applications in rectangular and exponential cases.

BOOKS FOR STUDY:

- 1) Modern probability theory by B.R. Bhat, Wiley Eastern Limited.
- 2) An introduction to probability theory and mathematical statistics by V.K.Rohatgi, John Wiley.
- 3) An Outline of statistics theory-1, by A.M.GOON, M.K. Gupta and B. Dasgupta, the World Press Private Limited, Calcutta.
- 4) The Theory of Probability by B.V. Gnedenko, MIR Publishers, Moscow.
- 5) Discrete distributions N.L. Johnson and S. Kotz, John wiley & Sons.
- Continuous Univariate distributions, vol.1&2- N.L.Johnson and S.Kotz, John Wiley & Sons.
- 7) Mathematical Statistics Parimal Mukopadhyay, New Central Book Agency (P) Ltd., Calcutta.

BOOKS FOR REFERENCES:

- 1) Billingsley, P. (1986): Probability and Measure. Wiley.
- 2) Kingman, J F C and Taylor, S. J. (1966): Introduction to Measure and Probability. Cambridge University Press.
- 3) David, H.A (1981): Order Statistics, 2nd Ed, John Wiley.
- 4) David H. A. and Nagaraja H.N.(2003): Order Statistics, 3/e, John Wiley & Sons.
- 5) Feller, W (1966): Introduction to probability theory and its applications, Vol.II, Wiley.
- 6) Cramer H (1946): Mathematical Methods of Statistics, Princeton

MAPPING	OF PROC	GRAM O	UTCON	IES WIT	H COUR	RSE OUT	COMES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	S	L	S	М	М
CO2	S	S	S	D	S	М	М
CO3	S	S	S		S	L	М
CO4	S	S	S	L	S	L	М
CO5	S	S	S	М	S	S	S
CO6	S	SS	S	М	S	S	S
CO7	S	S	M	-L	S	⇒ M	S



S 1.2 (22) :: STATISTICAL COMPUTING USING R

Credits: 4

COURSE OBJECTIVES:

- CO1: To expose the students to R- statistical programming language developed by scientists that has open source libraries for statistics, machine learning, and data science. It is a free software environment for statistical computing and graphics supported by the R Foundation for Statistical Computing.
- CO2: The student will learn a large coherent and integrated collection of statistical tools available in R. Further, the student will be familiar with graphical facilities for data analysis available in R.
- CO3: R is widely used by statisticians, data scientists and major corporations like Google, Airbnb, Facebook etc. for data analysis.
- CO4: R is well-developed, simple and effective programming language for data handling and storage facility.
- CO5: R is data analysis software includes a wide variety of functions, such as data manipulation, statistical modeling, and graphics. One really big advantage of R, however, is its extensibility. Developers can easily write their own software and distribute it in the form of add-on packages.

LEARNING OUTCOMES:

After learning the course the student

- LO1: Will be able to handle the data analysis using the R-statistical tools and can also perform graphical presentation of the data.
- LO2: Will be able to write own R-scripts for handling the data analysis in their own way.
- LO3: Has better job potentiality to acquire opportunities as data analyst in software companies, clinical trial data analysis companies and etc.

UNIT – I:

Introduction to R language: Objects (Atomics) -Basic types, modes and attributes, comments, constants. R–Data Types: character, numeric, integer, logical, complex and raw data types. R–Operators: arithmetic, relational, logical, assignment and miscellaneous operators. R–Variables: variable assignment, data type, finding variables using ls()function, deleting Variables using rm() function, R-I/O console functions-scan(), print(), cat(), format(), setwd() and getwd() functions. R-vectors: creating vectors, vector assignment, manipulating vectors, arithmetic, generating regular sequences, logical vectors, and character vectors using strsplit(), paste(), grep(), gsub() functions; R-factors: creating factor variables, handling factor data, generating factor levels using gl() function.

UNIT – II:

R-Matrices: Creating matrices, arithmetic operators on matrices, matrix facilities, forming partitioned matrices, cbind() and rbind() functions, R-Lists: creating a list, naming, accessing and manipulating list elements, converting a list to a vector. R-Data frames: creation, adding

rows and variables to data frame, attach() and detach(), working with data frames, data reshaping. Reading and getting data into R using files: reading data and writing data from / to files of type CSV, EXCEL, text and other data type files using the save(), load(), read.csv() and read.table(),write.csv() and write.table() functions. Retrieving files using file.choose(), function.

UNIT – III:

R – Control Structures: Decision making-if, if-else, ladder if-else, nested if-else, and switch statements. Loops-repeat, while and for statements. Loop control statements -- break and next. R – Functions: function definition, function components, built-in functions, user-defined function, syntax of a function, function arguments, arguments matching, scope and evaluation, calling a function, one-line functions, using default values in functions. Built in R-functions and writing own R-functions or R-codes for small standard statistical problems like finding summary statistics, correlation, one-sample t-test, two-sample t-test and paired samples t-test, etc. Group manipulation using apply family of functions - apply, sapply, lapply and tapply.

UNIT – IV:

R-Probability Distributions: Computing values of pdf, cdf, quantile and generating samples for bionomial, poission, normal, exponential, Weibull and other prominent distributions using Built in R – functions. Plotting density and cumulative density curves for the distributions. Built in R-syntaxes for the Shapiro-Wilk test of normality, Kolmogorov-Smirnov test for one-sample and two-sample cases, Wilcoxon Mann-Whitney one-sample and two-sample Utests, chi-square tests for association and goodness of fit. Writing own R-functions or Rcodes: Fitting of binomial, Poisson, normal, exponential, Weibull and logistic distributions based on a given frequency data and test for goodness of fit. Solving a non-linear equation using Newton-Raphson method.

$\mathbf{UNIT} - \mathbf{V}$:

R-Graphics: Use of high-level plotting functions for creating histograms, scatter plots, boxwhisker plots, bar plot, dot plot, line charts using numeric data and categorical data, pie charts, bar Charts, Q-Q plot and curves. Controlling plot options using low-level plotting functions, adding lines, segments, points, polygon, grid to the plotting region; Add text using legend, text, mtex; and modify/add axes, putting multiple plots on a single page. Built in R – syntaxes for one-way ANOVA, two- way ANOVA.

BOOKS FOR STUDY:

- 1) Dr. Mark Gardener (2012): *Beginning R The Statistical Programming Language*, Wiley India Pvt Ltd.
- 2) W.N. Venables and D.M. Smith (2016): An Introduction to R
- 3) J.P. Lander (2014): R for Everyone, Pearson Publications
- 4) Garrrett Grolemund: *Hands-On Programming with R*

BOOKS FOR REFERENCES:

- 1) De Vries, A., and Meys, J. (2016). *R For Dummies*, Second Edition, John Wiley & Sons Private Ltd, NY
- 2) Crawley, M, J. (2007). The R Book, John Wiley and Sons Private Ltd., NY.

MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES									
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7		
CO1	S	S	S	S	М	S	S		
CO2	S	S	S	S	L	S	S		
CO3	S	S	S	S	М	S	S		
CO4	S	S	S	М	S	L	М		
CO5	S	S	S	М	L	М	М		



<u>S 1.3 (22) :: ESTIMATION</u>

Credits: 4

COURSE OBJECTIVES:

CO1: To introduce the concepts of Estimation.

CO2: Characteristic features of good estimator, properties of good estimator with examples.

CO3: To introduce the role and importance of C. R. Rao Inequality, Rao – Blackwell theorem, Lehmann-Scheffe theorem.

CO4: Different methods of estimation in point estimation and internal estimation.

CO5: To introduce concepts of Baye's estimation.

LEARNING OUTCOMES:

- **LO1:** The concepts in theory of estimation, properties of good estimator and Fisher-Neymann factorization theorem.
- **LO2:** Upon completion of this unit the student will be able to understand unbiasedness, UMVUE, consistency, Efficiency with CAN, CAUN estimators.
- **LO3:** By completing this unit the student will know the different methods of estimation for variables and attributes.
- **LO4:** At the end of this unit the student will distinguish the difference between point estimation and internal estimation.
- LO5: Construction of confidence intervals, also able to understand the concepts of Baye's estimation.

UNIT-I:

Concepts of population, parameter (scalar, vector), parametric space, sample, sample space, statistic, estimator, estimate, sampling distribution, standard error, etc. Problem of point estimation, properties of good estimator, sufficiency- concept with examples, distinction between joint density and likelihood function. Fisher Neyman Factorization theorem. Complete sufficiency-examples, Exponential class, Minimal sufficiency.

UNIT-II:

Unbiasedness-concept, examples, properties, LMVUE, UMVUE, regularity conditions, Cramer-Rao Inequality and condition(s) for existence equality, examples of construction of UMVUE using Cramer-Rao Inequality, Rao-Blackwell Theorem, Lehmann-Scheffe Theorem, Necessary and Sufficient condition for the existence of MVUE. Minimum Mean Square Error (MMSE) Estimation. Consistency-Concept and examples, necessary condition for the existence of consistent estimator, efficiency, asymptotic relative Efficiency (ARE), CAN, CAUN estimators.

UNIT-III:

Moment method of Estimation, ML method of Estimation, Percentile estimation, Minimum Chi- square and Modified Minimum Chi- square.

UNIT-IV:

Interval Estimation, Confidence level, Construction of Confidence intervals using pivots, shortest expected length, UMA, UMAU Confidence sets. Relationship between confidence estimation and testing of hypothesis. Priori and posteriori distributions, loss function, risk function, Minmax & Bayes Estimator.

UNIT-V:

Censored and truncated distributions: Type 1 and Type 2 Censoring for normal and exponential distributions and their MLE's. Interval estimation: Confidence Intervals, using pivots; shortest expected length confidence intervals.

BOOKS FOR STUDY:

- 1) Statistical Inference by H.C,. Saxena & Surendran.
- 2) An Introduction to Probability and Statistics by V.K.Rohatgi and A.K.Md.E.Saleh(2001).
- Mathematical Statistics- Parimal Mukopadhyay(1996), New Central Book Agency (P) Ltd., Calcutta.

BOOKS FOR REFERENCES:

- 1) An Outline of Statistical Theory, Vol.II by A.M.Goom, M.K. Gupta and B. Dasgupta (1980), World Press, Calcutta.
- 2) Linear Statistical Inference and its Application by C.R. RAO (1973), John Wiley.
- 3) A First Course on Parametric Inference by B.K. kale(1999) Narosa Publishing Co.,
- 4) Lehman, E. L., and Cassella, G. (1998). Theory of Point Estimation, Second Edition, Springer, NY.

MAPPING O	MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES										
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7				
C01	S	М	M	; సర్వ S ప్రతి	Jeger T	М	S				
CO2	S	S	S	S	L	S	М				
CO3	S	S	S	S	М	S	S				
CO4	S	S	S	L	М	L	М				
CO5	S	S	М	М	L	М	L				

<u>S 1.4 (A) (22) :: SAMPLING THEORY</u>

Credits: 4

COURSE OBJECTIVES:

- CO 1: Able to understand the basic concepts of various probability sampling techniques.
- CO 2: Understand the selection of PPS sampling and able to calculate the Des Raj, Murthy's estimator Horvitz Thompson estimator.
- CO 3: Able to estimate population mean and variance of systematic sample when population exhibits linear trend.
- CO 4: Understand Cluster sampling and their applications by estimation of population mean and variance.
- CO 5: Able to apply two stage sampling technique and also Two-stage PPS sampling technique.
- CO 6: Understand the concept of ratio and regression methods of estimation in stratified random sampling.
- CO 7: Acquainted with multiphase and multistage sampling.

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO1: Acquire knowledge to assess different sampling methods and their applications
- LO2: Students acquire the basic knowledge to understand different advanced techniques of sampling methods.
- LO3: To explain and to compare various allocations using stratified random sampling.
- LO4: To use practical applications of ratio and regression method of estimation.
- LO5: Students acquire the theoretical as well as practical knowledge of field study to analyze the data, interpret the results and draw valuable conclusions.

UNIT-I:

Systematic Sampling: Allocation problem in stratified sampling, gain in precision due to stratification, estimation of sample size with continuous data, stratified sampling for proportions, Methods of populations with linear trend: Yates end correction, Modified systematic sampling, balanced systematic sampling, centrally located sampling, circular systematic sampling.

UNIT-II:

Varying probability and Cluster sampling: Cluster sampling with equal and unequal cluster sizes, optimum cluster size for fixed cost. PPS sampling with and without replacements, procedures of selection of a sample, estimator of population total and its sampling variance in PPS with replacement, Des Raj and Murthy's estimator (for sample size two), Horvitz-Thomson estimator, Grundy's estimator, Midzuno-Sen Sampling Scheme.

UNIT-III:

Two-stage sampling: Two-stage sampling with equal number of second stage units, estimation of population mean, its variance and estimation of variance. Double sampling (two phase sampling) for stratification, variance of the estimated mean, optimum allocation in double sampling.

UNIT-IV:

Multiphase Sampling: Introduction, Double sampling for Difference estimation. Double sampling for ratio estimation. Double sampling for regression estimator, Optimum allocation varying probability sampling. Non sampling errors: Sources and types of non Sampling errors, Non response errors, techniques for adjustment of non response, Hansen and Hurwitz Technique, Deming's Model.

UNIT-V:

Ratio Estimator: Introduction, Bias and Mean square error, Estimation of variance, confidence interval, comparison with mean per unit estimator, Ratio estimator in stratified random sampling. Difference estimator and Regression estimator: Introduction, Difference estimator, Difference estimator in stratified sampling. Regression estimator, Comparison of regression estimator with mean per unit estimator and ratio estimator. Regression estimator in stratified sampling.

BOOKS FOR STUDY:

- 1) Sampling techniques by W.G. Cochran, John Wiley
- 2) Sampling theory by Singh & Chaudhary
- 3) Sampling Theory, Narosa Publication by Des Raj and Chandok (1998)
- 4) Sampling Theory and Methods, Narosa Publishers by S. Sampath (2001)
- 5) Theory and Analysis of Sample Survey Designs, F.S. Chaudhary: New Age International Publishers, Delhi.

BOOKS FOR REFERENCES:

- 1) Sampling Theory & Methods by M.N. Murthy.
- 2) Sampling theory of surveys with Applications: P.V.Sukhatme & B.V. Sukhatme.
- 3) Theory and methods of survey sampling. Mukhopadhyay(1988).

MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES										
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7			
CO1	S	S	M	సి సెట్నం ప్రక	a S	М	S			
CO2	S	S	Μ	L	S	S	S			
CO3	S	S	Μ	L	S	S	L			
CO4	S	S	М	S	S	L	М			
CO5	S	S	S	М	S	М	М			
CO6	S	S	Μ	S	S	L	М			
CO7	S	S	S	М	S	М	М			

<u>S 1.4 (B) (22) :: LINEAR ALGEBRA</u>

Credits: 4

COURSE OBJECTIVES:

- CO 1: To prepare the students about algebra of matrices and vector spaces.
- CO 2: To explain about characteristic roots and vectors and linear transformations with examples.
- CO 3: To prepare the students on the concept of the orthonogonality and quadratic forms.
- CO 4: To prepare the students to understand Cayley Hamilton theorem.
- CO 5: To Make the students to understand the concept of the spectral decomposition of the matrices.

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO 1: Students understand elementary transformations in a matrix and their solutions.
- LO 2: Students learn characteristic roots and vectors with numerical examples. They also know theoretical proofs of theorems.
- LO 3: Discriminate between diagonalizable and non-diagonalizable matrices; orthogonally diagonalizable symmetric matrices and quadratic forms
- LO 4: Students understand and apply Cayley Hamilton theorem.
- LO 5: Understand the concept of the spectral decomposition of the matrices.

UNIT-I

Algebra of matrices; Elementary transformations; Rank and Inverse of a matrix; Nullity; Partitioned matrices; Kronecker product; Generalized inverse of matrix; Moore-Penrose generalized inverse; Solutions of simultaneous equations.

UNIT-II

Finite dimensional Vector Spaces; Vector Spaces and Subspaces; Linear dependence and independence; Basis and dimension of a vector space; Completion theorem.

UNIT-III

Inner product Spaces; Orthonormal basis and Gram-Schmidt orthogonalization process; Orthogonal projection of a vector. Linear transformations and properties; Orthogonal and unitary transformations; Real quadratic forms.

UNIT-IV

Reduction and classification of quadratic forms; Hermitian forms; Sylvesters law of inertia; Canonical reduction of quadratic form. Characteristic roots and vectors; Cayley – Hamilton theorem.

UNIT-V

Minimal polynomial; Similar matrices; Spectral decomposition of a real symmetric matrix; Reduction of a pair of real symmetric matrices; Hermitian matrices.

BOOKS FOR STUDY:

- 1) Campbell, H.G. (1980), Linear Algebra with Applications, 2nd Edition, Prentice-Hall, Englewood Cliffs (new Jersey), 1980.
- 2) Hadley, G. (1987), Linear Algebra, Narosa Publishing House.
- 3) Rao, A.R. and Bhimasankaram, P. (1992), Linear Algebra, Tata McGraw Hill Publishing Company Ltd.

BOOKS FOR REFERENCES:

- 1) Graybill, F.A. (1983). Matrices with applications in statistics, 2nd ed. Wadsworth, Belmont (California).
- 2) Rao, C. R. (1985). Linear statistical inference and its applications, Wiley Eastern Ltd., New Delhi.
- 3) Searle, S. R. (1982). Matrix Algebra useful for Statistics, John Wiley and Sons. Inc.
- 4) Bellman, R. (1970), Introduction to Matrix Analysis, 2nd ed. McGraw Hill, New York.
- 5) Biswas, S. (1984), Topics in Algebra of Matrices, Academic Publications.
- 6) Halmos, P.R. (1958), Finite-dimensional Vector Spaces 2nd ed. D.Van Nostrand Company, Inc.
- 7) Hoffman, K. and Kunze, R, (1971). Linear Algebra, 2nd ed., Prentice Hall
- 8) Rao, C.R. and Mitra, S.K. (1971), Generalized Inverse of Matrices and its Applications, John Wiley and Sons, Inc.
- 9) Narayan, S. (1970), Theory of Matrices, S. Chand & Company, New Delhi.

MAPPING	MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES										
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7				
CO1	S	S	S	M	S	S	L				
CO2	S	M	S	M	S	S	М				
CO3	S	S	Sta	М	55 S	S	М				
CO4	S	М	S	S	S	L	L				
CO5	М	М	S	М	S	М	L				



M.Sc. STATISTICS

SEMESTER-II

<u>S 2.1 (22) :: MULTIVARIATE ANALYSIS</u>

COURSE OBJECTIVES:

- **CO1:** To acquaint the students the multivariate normal (MVN) distribution properties and estimation of the parameters of MVN populations.
- **CO2:** To acquaint the students with the applications of Hotelling T^2 Statistic and Mahalanobis D^2 statistic in case of one sample, two samples and paired samples drawn from MVN populations.
- **CO3:** To explore the students with application of Multivariate analysis of variances (MANOVA) for one way classification multivariate data.
- **CO4:** To explore the students with application of principal component analysis (PCA), discriminant analysis, cluster analysis, factor analysis.

LEARNING OUTCOMES:

After successful completion of the course the student will be able

- **LO1:** To apply Hotelling T² Statistic and Mahalanobis D² statistic for testing the equality of two MVN population mean vectors in two samples and paired samples drawn from MVN populations.
- LO2: To carry out one-way (MANOVA) for one way classification multivariate data.
- **LO3:** To explore the students with application of principal component analysis (PCA), discriminant analysis, cluster analysis, factor analysis and interpret results from multi dimensional scalling.
- **LO4:** Understand the various hierarchical and non-hierarchical clustering methods and their applications.
- **LO5:** Use of popular statistical packages in analyzing the real data sets.

UNIT-I:

The multivariate normal distribution and estimation: The multivariate normal distribution and its properties. Characteristic function of multivariate normal distribution. Sampling from multivariate normal distribution and maximum likelihood estimation, sampling distributions of Sample mean and sample covariance matrix. **UNIT-II:**

Inference: Wishart's distribution and it's properties. Definition of Hotelling's T^2 -distribution (statistic). Invariance property of Hotelling's T^2 -statistic. Application of T^2 statistic in tests of mean vector(s) in case of one and two multivariate normal populations.

The likelihood ratio principle. Mahalanobis D^2 -statistic and it's relation with T^2 -statistic. Multivariate analysis of variances (MANOVA) for one way classification.

Credits: 4

UNIT-III:

Discriminant Analysis: Classification and discrimination procedures for discrimination between two multivariate normal populations, Fisher's discriminant function–separation of two multivariate populations. Classification with several multivariate normal populations. Fisher's method for discrimination among several multivariate populations.

UNIT-IV:

Cluster Analysis: Similarity measures, Euclidian distance and Mahalanobis squared distance- D^2 between two p-dimensional observations (items). Hierarchical Clustering methods - Single Linkage, Complete Linkage, Average Linkage, Ward's method and Centroid Linkage methods. Non-Hierarchical Clustering methods-K-Means method. Multidimensional scaling.

UNIT-V:

Special topics: Principle components analysis - definition, derivation, properties and Computation. Canonical variates and canonical correlations - definition, derivation and computation. Factor Analysis - Orthogonal factor model, Methods of estimating factor loadings - the principal component method and maximum likelihood methods of estimation. Factor rotation: orthogonal factor rotation, varimax rotation.

BOOKS FOR STUDY:

- 1) Anderson, T.W.(2000). An Introduction to Multivariate Statistical Analysis, 3rd Edition, Wiley Eastern
- 2) Johnson, A. and Wichern, D.W.(2001). *Applied Multivariate Statistical Analysis*, Prentice Hall and International Mardia, K.V. *Multivariate Analysis*

BOOKS FOR REFERENCES:

- 1) Gin. N. C. (1977): *Multivariate Statistical Inference*. Academic Press
- 2) Seber, G. A. F. (1984): Multivariate Observations. Wiley
- 3) Kshirsagar, A. M. (1972): Multivariate Analysis, Marcel Dekker
- 4) Morrison. D. F. (1976): *Multivariate Statistical Methods*, 2nd Ed. McGraw Hill
- 5) Muirhead, R. J. (1982): Aspects of Multivariate Statistical Theory, J. Wiley
- 6) Rao, C. R. (1973): Linear Statistical Inference and its Applications, 2nd ed. Wiley
- 7) Sharma. S. (1996): Applied Multivariate Techniques, Wiley
- 8) Srivastava, M. S. and Khatri, C. G. (1979): An Introduction to Multivariate Statistics, North Holland.

MAPPING OF PROGRAM OUTCOMES WITH COURSE										
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7			
CO1	S	S	S	М	L	S	S			
CO2	S	S	М	S	L	М	М			
CO3	S	S	М	S	L	М	L			
CO4	S	S	S	S	L	S	L			

S 2.2 (22) :: TESTING OF HYPOTHESIS

Credits: 4

COURSE OBJECTIVES:

- **CO1:** Draw inference about unknown population parameters based on random samples
- **CO2:** Impart knowledge on statistical hypothesis.
- **CO3:** Understand Neyman-Pearson fundamental lemma for testing statistical hypothesis.
- CO4: Understand the test procedures MPT, UMPT, LMPT, LRT and SPRT.
- CO5: Inculcate various parametric and non-parametric, sequential test procedures.

LEARNING OUTCOMES:

- **LO1:** Upon completion of this unit the student will be able to understand the concepts and procedures of testing of hypotheses.
- LO2: Generalization of Neymann Pearson-Lemma and different Uniformly Most Powerful Test will also be get acquainted.
- **LO3:** After completing this unit, the student will understand the Neymann structure and Likelihood ratio test with properties.
- **LO4:** This unit provides and understanding for the student to distinguish between parametric and non-parametric tests in this unit several non-parametric tests will be understand able to the student.
- **LO5:** This unit provides and understanding for the student to distinguish between parametric and non-parametric tests in this unit several non-parametric tests will be understand able to the student.
- **LO6:** At the end of this unit the student will understand the notion of SPRT, and its applications to different distributions.

UNIT-I:

Tests of hypotheses, concept of critical region, critical function, two kinds of errors, power function, level of significance, MP and UMP tests, Neyman Pearson lemma, Randomized and Non Randomized tests.

UNIT-II:

Generalized NP-lemma, UMP tests for simple null hypothesis against one sided alternatives, and for one sided null against one sided alternative in one parameter exponential family, extension of these results to distributions with MLR property, nonexistence of UMP test for simple null against two sided alternatives in one parameter exponential family.

UNIT-III:

UMP unbiased tests and LMP tests. Similar regions, Neyman structure, Likelihood ratio test, properties of LR test, asymptotic distribution of LR test.

UNIT-IV:

Chi-square and kolmogorov Smirnov tests for goodness of fit, Kendall's tau statistic, Kruskal-Wallis test, Friedman's two-way analysis of variance by ranks, Bartlett's test for

homogeneity of variances, chi-square test for homogeneity of correlation coefficients, F-test for homogeneity of regression coefficients, variance stabilizing transformation and large sample tests.

UNIT-V:

Notion of sequential tests, SPRT, Wald's fundamental identity, relation between the quantities A,B, alpha and beta, OC and ASN functions of SPRT, application to binomial, Poisson and normal distributions, efficiency of a sequential test.

BOOKS FOR STUDY:

- 1) Statistical Inference by H.C, Saxena & Surendran
- 2) An outline of Statistical Theory vol.2 by A.M. Goon and B. Das Gupta.
- 3) An Introduction to probability and Mathematical Statistics by V.K. Rohatgi.
- 4) Mathematical Statistics- Parimal Mukopadhyay(1996), New Central Book Agency (P)Ltd., Calcutta.

BOOKS FOR REFERENCES:

- 1) Advanced Theory of Statistics VOL.II by M.G. Kendall & A. Stuart.
- 2) Introduction to Mathematical Statistics by R.V. Hogg & A.T. Craig.
- 3) Linear Statistical Inference and applications by C.R. Rao.

63

MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES										
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7			
CO1	S	S	S	M	M	S	S			
CO2	S	S	S	М	S	М	S			
CO3	S	S	М	S	S	М	L			
CO4	S	S	M	S	S	S	L			
CO5	S	S	М	М	S	S	L			

S 2.3 (22) :: THEORY OF LINEAR ESTIMATION AND ANALYSIS OF VARIANCE

Credits: 4

COURSE OBJECTIVES:

- **CO1:** This course provides the students the ability to understand the design and conduct experiments, as well as to analyze and interpret data.
- **CO2:** To learn the basic principles in the Design of simple experiments.
- CO3: To learn different tests experiments of Analysis of variance and covariance
- CO4: To learn about missing plot techniques of CRD, RBD, LSD.

LEARNING OUTCOMES:

After studying the course the students should be able to carry-out:

- **LO1:** Important characteristics of matrices, such as determinant, rank, eigen values, eigen vectors and Quadratic forms.
- LO2: Students will also be able to use characteristics of a matrix to solve a Theory of linear system of equations, BLUE and Gauss-Markov theorem etc.,
- **LO3:** Apply different test experiments of analysis of variance for one way, two –way classification and mixed effect models.
- **LO4:** Understand make use of analysis of covariance-one way, two-way classification and Learn about missing plot techniques of RBD, LSD.

UNIT-I:

Matrix algebra- Fundamental definitions, determinants, rank of a matrix, inverse of a matrix, orthogonal matrix, idempotent matrix, characteristic roots and vectors of a matrix. Numerical computation of characteristic roots and vectors for a positive definite matrix. Reduction of a positive definite matrix to a diagonal form using an Orthogonal matrix and non-singular matrix. Cauley-Hamilton theorem, trace of a matrix. Quadratic forms, reduction of quadratic forms using orthogonal transformation, statement of Cochran's theorem for quadratic forms.

UNIT-II:

Theory of linear estimation, linear models, estimability of linear parametric function, best linear unbiased estimator, Gauss-Markov set-up, Gauss-Markov theorem, generalized linear model, generalized Gauss-Markov theorem (Atken's theorem).

UNIT-III:

Decomposition of sum of squares in analysis of variance one way classification, two way classification with equal and unequal number of observations per cell. Multiple comparisons; Fisher's least significance difference test and Duncan's multiple range test, Fixed, random and mixed effect models.
UNIT-IV:

Analysis of covariance of one way and two way classification, applications to standard designs- CRD,RBD missing plot technique- general theory and applications to RBD and LSD.

UNIT-V:

Model Adequacy checking: Test for Normality, Test for equality of Variances (Bartlett test, Modified Levene Method). Multiple comparison tests: Turkey's test, The Fisher Least significant Difference (LSD) method, Duncan's Multiple range test.

BOOKS FOR STUDY:

- 1) Montgomery, D.C, (1976), Design and Analysis of experiments., John Wiley & sons.
- 2) Joshi, D.D.(1987), Linear Estimation and Design of experiments., Wiley Eastern Ltd.
- Das, M.N. and Giri, N.C. (1986), Design and An Analysis of Experiments, Wiley Eastern Ltd.

BOOKS FOR REFERENCES:

- 1) Datta, K.B. (2000)., Matrix and Linear Algebra
- Rangaswamy, R, (1995), A text book of Agricultural Statistics., New Age international Publishers Limited.
- 3) Kempthorne, O, (1951)., The design and Analysis of Experiments., Wiley Eastern Private Limited.
- 4) Rao, C.R, (1983)., Linear Statistical inference and its applications., Wiley Eastern Ltd.
- 5) Raghavarao, D.(1987), statistical Techniques in Agricultural and Biological Research., Oxford & IBH publishing Company Private limited.
- 6) Federer, W.t (1967), Experimental Design Theory and Application, Oxford & IBH publishing company.
- 7) Biswas, S. (1984). Topics in Algebra of Matrices, Academic Publication.

MAPPING	MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES										
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7				
CO1	S	S	S	S	L	S	L				
CO2	S	S	S	S	L	М	М				
CO3	S	S	М	S	L	L	S				
CO4	S	М	S	S	M	S	L				

S 2.4 (A) (22) :: STOCHASTIC PROCESSES

Credits: 4

COURSE OBJECTIVES:

- **CO1:** Understand the meaning of stochastic process along with classification of stochastic processes, Fine state Markov chains, classification of states of a Markov chain, limiting and stationary distribution of a Markov chain.
- **CO2:** Understand homogeneous Poisson process, non homogeneous Poisson process, Compound Poisson process and important properties of these processes, pure birth process, pure death process, general birth-death process.
- **CO3:** Understand renewal process, elementary renewal theorem, black well's and smith's renewal theorem, central limit theorem for renewals.
- **CO4:** Understand Galton-Watson branching process and associated generating functions and their relations, probability of ultimate extinction of a branching process.
- **CO5:** Understand the stochastic models of Brownian Motion, Limit of Random Walk, Martingale Processes applications and it's properties.

LEARNING OUTCOMES:

At the end of this Course Students will be able:

LO1: Acquired Knowledge about Different Types of Stochastic Processes

LO2: To use birth and death Poisson processes whenever necessary

LO3: To know the concept of renewal process and its applications

LO4: To know the concept of branching process and to compute extinction probabilities

LO5: To apply Browning motion in finance problems.

UNIT-I:

Stochastic Processes Preliminaries: Introduction to stochastic processes (sp's); classification of sp's according to state space and time domain, countable-state Markov chains (mc's). Chapman-kolmogrov equation, calculation of n-step transition probability and its limit. Classification of states.

UNIT-II:

Markov Process: Markov processes with discrete state space, Poisson process, postulates of Poisson process, properties of Poisson process, Poisson process and related distributions – interval time – further interesting properties of Poisson process, generalizations of Poisson process – Poisson process in higher dimensions-Poisson cluster process – pure birth process - birth – immigration process – time dependent Poisson processes – random variation of the parameter λ , birth and death process – birth and death rates.

UNIT-III:

Renewal Process: Renewal processes in discrete time - relation between F(s) and P(s), renewal interval, renewal theory in discrete time, renewal theorem.

Renewal process in continuous time- renewal function and renewal density, renewal equation. Stopping time, Wald's equation. Elementary renewal theorem, Black well's and smith's renewal theorem, Central limit theorem for renewals.

UNIT-IV:

Branching Process: Branching processes, properties of generating functions of branching processes- moments of X_n ; probability of extinction – asymptotic distribution of X_n ; Distribution of the total number of progeny.

UNIT-V:

Brownian Motion: Limit of Random Walk, Martingale Processes applications and it's properties. Brownian Motion Process applications and it's properties.

BOOKS FOR STUDY:

- 1) Medhi, J. (1982): Stochastic processes, second edition, new age international (p) Ltd.
- 2) Karlin, s and Taylor, H.M.(1975); *A first course in stochastic process* vol.1. academic press
- 3) Bhat, U.N. (1984); *Elements of applied stochastic processes*, John Wiley and sons
- 4) Ross .(1995); Stochastic processes, John Wiley and sons
- 5) Basu, A.K.(2003), *Introduction to Stochastic Process*, Narosa Publishing House, New Delhi.

BOOKS FOR REFERENCES:

- 1) Adke, S.R. and Manjunath, S.M. (1984): *An Introduction to Finite Markov Processes*, Wiley Eastern
- 2) Cinlar, E. (1975): Introduction to Stochastic Processes, Prentice Hall
- 3) Feller, W. (1968): Introduction to Probability and its Applications, Vol. 1, Wiley Eastern
- 4) Hoel, P.G. Port, S.C. & Stone, C.J. (1972). *Introduction to Stochastic Processes*, Houghton Mifflin
- 5) Serfozo, R. (2009). Basics of Applied Stochastic Processes, Springer.

MAPPING O	MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES											
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7					
CO1	S	S	М	L	S	М	S					
CO2	S	S	М	L	S	М	S					
CO3	S	S	Μ	L	S	М	S					
CO4	S	S	М	L	S	S	S					
CO5	S	S	М	L	S	S	S					

<u>S 2.4 (B) (22) : LINEAR MODELS AND APPLIED REGRESSION</u> <u>ANALYSIS</u>

Cridits:4

COURSE OUTCOMES:

- **CO1:** Able to calculate least square estimates of Gauss-Markov model.
- **CO2:** Able to obtain estimates in case of correlated observations.
- **CO3:** Able to test hypothesis for linear parametric functions.
- **CO4:** To be able to deal with multiple regression analysis.
- **CO5:** Able to estimate regression coefficient under multicollinearly.

LEARNING OUTCOMES:

LO1: Able to get theoretical foundation for linear estimation theory and regression analysis.

- **LO2:** Able to demonstrate the least square estimates of the parameters and their statistical significance.
- LO3: Acquainted with different regression techniques that can be used in statistical analysis.
- LO4: To perform Analysis of Variance and to construct confidence intervals and regions.

LO5: Expertise with different methods for estimating and testing the relationships between independent and dependent variables.

UNIT-I

Gauss-Markov set-up, Normal equations and Least squares estimates, variances and covariances of least squares estimates, estimation of error variance.

UNIT-II

Estimation with correlated observations, least squares estimates with restriction on parameters, simultaneous estimates of linear parametric functions.

UNIT-III

Tests of hypotheses for one and more than one linear parametric functions, confidence intervals and regions. Analysis of Variance.

UNIT-IV

Simple linear regression, multiple regression, fit of polynomials and use of orthogonal polynomials.

UNIT-V

Multicollinearity, Ridge regression and principal component regression, subset selection of explanatory variables.

BOOKS FOR STUDY:

- 1) Graybill, F.A. (1983): Matrices with Applications in Statistics. Wadsworth.
- 2) Draper, N.R. and Smith, H (1998): Applied Regression Analysis. 3rdEdition. Wiley-Blackwell.
- Douglas C. Montgomery, Elizabeth A. Peck and G. Geoffrey Vining (2012): Introduction to Linear Regression Analysis – 5th Edition. Wiley
- 4) Goon, Gupta and Das Gupta (2003): An outline of Statistical Theory. Volume II. The World Press Pvt. Ltd.

BOOKS FOR REFERENCES:

- 1) Bapat.R.B. (2012): Linear Algebra and Linear Models. 3rd Edition. Springer.
- Cook, R.D. and Weisberg, S. (1983): Residual and Influence in Regression. 1st Edition. Chapman and Hall.
- 3) Johnson, J. (1996): Econometric Methods, 4th Edition. McGraw Hill.
- Rao, C.R. (2002): Linear Statistical Inference and Its Applications. 2nd Edition. Wiley-Blackwell.
- 5) Weisberg, S. (2013): Applied Linear Regression. 4th Edition. Wiley.

MAPPING (OF PROC	GRAM (DUTCON	AES WIT	TH COUR	RSE OUT	COME
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	S	M	M	Š	S
CO2	S	S	S	S	S	S M	М
CO3	S	S	P	S L	M	М	L
CO4	S	М	М	S	S	S	L
CO5	S	S	S	М	L	S	M



M.Sc. STATISTICS

SEMESTER-III

S 3.1 (22) :: DESIGN OF EXPERIMENTS

Credits: 4

COURSE OUTCOMES:

- CO1: To understand ANOVA, ANCOVA, fixed and random effect models
- CO2: To understand the concepts of CRD, RBD, LSD and their missing plot techniques
- CO3: To construct the multiple comparison tests and split plot design
- CO4: To summarize the analysis of 2ⁿ and 3² factorial designs and able to test their Significance
- CO5: To Familiarize with total and partial confounding
- CO6: To construct BIBD and PBIBD and to perform their analysis

LEARNING OUTCOMES:

- LO1: Acquire theoretical foundations for design and analysis of experiments.
- LO2: Able to apply ANCOVA technique.
- LO3: Expertized in analysis of experiments and perform the data analysis using CRD, RBD and LSD even in case of missing values and capable of testing the model adequacy.
- LO4: Expertize in analyzing factorial designs and estimate factorial effects and test their significance. Experiment confounding techniques to real life problems.
- LO5: Able to apply the Youden square design and intra block analysis for estimating the Parameters of BIBD and PBIBD.
- LO6: Expertized in applying different analysis of variance techniques in agricultural business and industries.

UNIT-I:

General factorial experiments, factorial effects, best estimates and testing the significance of factorial effects, estimation of main effects, interaction and analysis of 2^n factorial experiments in general with particular reference to n=2,3. 3^2 and 3^3 factorial experiments. Total and partial confounding in case of 2^n (for n=2,3), 3^2 and 3^3 factorial designs.

UNIT-II:

Incomplete block designs; balanced Incomplete block designs (BIBD), parametric relations, intra block analysis, simple methods of constructions of BIBD, resolvable and affine resolvable designs, Partially Balanced Incomplete Block Designs (PBIBD) with two associate classes, parametric relations, intra block analysis.

UNIT-III:

Youden square design, simple lattice design, split plot design, strip plot design and their analysis, Gracco latin square design.

UNIT-IV:

Concept of response surface methodology (RSM), response surface designs, linear response surface designs, second order response surface designs, variance of estimated second order response surface, Rotatable designs; conditions for second order rotatable designs, construction of second order rotatable designs using central composite designs, Balanced incomplete block designs.

UNIT-V:

Taguchi Method, Taguchi Philosophy, Loss Functions, Signal-to-Noise Ratio and Performance Measures, Critique of S/N Ratios. Experimental Design in the Taguchi Method. Parameter Design in the Taguchi Method.

BOOKS FOR STUDY:

- 1) M.N. Das and N.C. Giri. (1986), Designs and Analysis of Experiments, Wiley Eastern Ltd.
- 2) Montgomery, D.C, (1976)., Design and Analysis of Experiments, John Wiley & sons.
- 3) D.D.Joshi. (1987), Linear Estimation and Design of Experiments, Wiley Eastern Ltd.
- 4) Taguchi Engineering by Philippe ross.

BOOKS FOR REFERENCES:

- 1) Raghavarao, D. (1971), Constructions and Combinatorial Problems in Design of Experiments, John Wiley & Sons, Inc.
- 2) W.G. Cochran and G.M. Cox, (1957), Experimental designs, A wiley International Edition.
- 3) Box, G.E.P. and Draper, N.R. (1986), Empirical Model- Building and Response surfaces, John Wiley & Sons.
- 4) R.H. Myers. (1976), Response Surface Methodology, Allyn and Bacon, Boston
- 5) Aloke Dey. (1986), Theory of Block Designs, Wiley Eastern Limited.
- 6) Oscar Kempthorne (1951), The Design and Analysis of Experiments., Wiley Eastern Private Limited.
- 7) Walter T.Federer (1967)., Experimental Design Theory and Application., Oxford & IBH Publishing Company.

MAPPING OF	F PROG	RAM OU	UTCOM	ES WITH	I COUR	SE OUTC	OMES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	S	Μ	S	S	Μ
CO2	S	М	S	S	М	S	L
CO3	S	S	S	S	S	М	L
CO4	S	S	S	S	М	М	L
CO5	S	S	L	S	L	S	S
CO6	S	L	М	S	S	М	S

S 3.2 (22) :: STATISTICAL QUALITY CONTROL

Credits: 4

COURSE OUTCOMES:

- CO1: Able to understand basics of production process monitoring and apply concept of control charts to it.
- CO2: Able to implement response surface methodology in quality control.
- CO3: Acquainted with Six Sigma and lean thinking in industrial experimentation.

LEARNING OUTCOMES:

- LO1: Can identify the cause of defects using statistical quality management techniques.
- LO2: Able to apply statistical quality control techniques to minimize the variability in manufacturing and business process.
- LO3: Expertise in the most import field of applied statistics that contributes to quality control in all most all industries.

UNIT – I:

The \overline{X} and S control charts with variable sample size. The S² control chart. The Shewart Control Chart for individual measurements. Control charts for multiple stream process and group control charts. Economic design of control charts: designing a control chart, process characteristics, cost parameters, early work & semi-economic designs and an economic model of the \overline{X} control chart.

UNIT – II:

The Cumulative Sum (CUSUM) control chart - Basic principles, the tabular or algorithmic CUSUM for monitoring the process mean, recommendations for CUSUM design. The standardized CUSUM, rational subgroups, one sided CUSUMs, CUSUM for monitoring process variability, CUSUMs for other sample statistics. The V-Mask procedure. The exponentially weighted moving average (EWMA) control chart - Design of a EWMA control chart, rational sub group, robustness of the EWMA to non-normality, extension of the EWMA. The moving average control chart.

UNIT – III:

Statistical process control for short production runs - \overline{X} and R charts for short production runs, attribute control charts for short production runs. Modified and acceptance control charts - modified control limits for \overline{X} chart, acceptance control charts, control chart for a "Six-Sigma" process.

UNIT – IV:

The multivariate process monitoring and control: description of multivariate data, the multivariate normal distribution, the sample mean vector and covariance matrix. The Hotelling T^2 control chart. The multivariate exponential weighted moving average (EWMA) control chart. Control chart for monitoring variability. Latest structure methods: principal component and partial least squares.

$\mathbf{UNIT} - \mathbf{V}$:

Tools and Techniques of Total Quality Management (TQM), techniques for analyzing a quality process, SPC as a tool of quality management, Quality systems – ISO 9000 standards, QS-9000 standards, Bench marking practices and Quality Auditing Notion of Six – sigma and its uses.

BOOKS FOR STUDY:

- 1) R.C. Guptha(2001): Statistical Quality Control. 9th Edition. Khanna Publishers.
- 2) Duncan Acheson (1986): Quality Control and Industrial Statistics. 5th Edition. Irvin.
- Statistical Quality Control 7th edition, E.L. Grant & R.S. Leavenworth; McGraw Hill, New York.

BOOKS FOR REFERENCES:

- 1) Cowden D J (1957): Statistical Methods in Quality Control. 1st Edition. Prentice-Hall Inc.
- 2) Mittag and Rinne (1993): Statistical Methods for Quality Assurance. 2nd Edition. Chapman and Hall Ltd.
- Montgomerv. D.C (2012): Introduction to Statistical Quality Control. 7th Edition. John Wiley and Sons.

MAPPING	OF PRO	GRAM (DUTCO	MES WIT	TH COU	RSE OUT	COMES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	S	S	М	М	S
CO2	S	S	L	S	S	М	S
CO3	S	М	S	S	L	L	S

S 3.3 (A) (22) :: ACTUARIAL STATISTICS

Credits: 4

COURSE OBJECTIVES:

- CO1: To introduce and expose students to application of statistics in actuarial field.
- CO2: To understand the basic concepts and statistical methods applicable in actuarial science
- CO3: To provide an exposure to the basic models of insurance processes
- CO4: To learn the concept of interest, different life insurance products, life annuities, net premiums etc.,

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO1: To equipped with the advanced concepts which is required for internship in research institutes working in financial domain
- LO2: Get expertise in the with the role of insurance in society, basic economic theory, and the basics of how insurance is required for applications in real time financial data like stock market
- LO3: When uncertainty involved, student can develop and analyze actuarial models with the help of probability theory, statistics and economic theories.
- LO4: Have familiarity with several of the technical tools, computer languages or software packages used by actuaries.
- LO5: Develop communication, leadership and teamwork skills, and understand their importance in the actuarial industry.
- LO6: It gives the ideas of entrepreneurship and also allows the students to work as a statistical advisor in insurance company, policy makers, Banking Domain.

UNIT-I:

Effective Rate of interest - Nominal rate of interest - Force of interest Effective rate of interest corresponding to Nominal rate of interest and Force of interest - Accumulation of 1 unit corresponding to the given rate of interest present value of 1 unit due at the end of n years corresponding to the given rate of interest, effective rate of discount-Nominal rate of discount – Force of interest varying continuously.

UNIT-II:

Definition of Annuity - Present value and Accumulation of an Immediate annuity - Annuity due - Present value and Accumulation of an Annuity – due - Present value and Accumulation of a Perpetuity and Perpetuity - due-Increasing and Decreasing Annuities. Annuities where payments are in A.P. Annuities where payments are made continuously.

UNIT-III:

Analysis of Annuity payments - Loan installment - Principal and interest portions of a typical loan installment – General Expression for principal and interest portion – Purchase price of an annuity net of tax. Independent annual interest rates - Mean and Variance of the accumulation of a single investment, viz $E(S_n)$ and $V(S_n)$ – Mean and Variance of the accumulation of a series of investments, viz $E(A_n)$ and $V(A_n)$ - Mean and Variance of a present value of unit due at the end of n years, viz $E(V_n)$ and $V(V_n)$. Dependent annual interest rates and simple problems.

UNIT-IV:

Net present value (NPV) - Internal rate of return (IRR)- Interpretation of NPV and IRR- Comparison of two investment projects - Discounted Payback Period - The effect of inflation on IRR- Money weighted rate of return (MWRR) - Time weighted rate of return (WRR) - linked internal rate of return (LIRR).

UNIT-V:

Multiple life functions, joint life and last survivor status, insurance and annuity benefits through multiple life functions, evaluation for special mortality laws. Multiple decrement models, deterministic and random survivorship groups, associated single decrement tables, central rates of multiple decrements, central force assumptions for multiple decrements. Uniform distribution assumption for multiple decrements.

BOOKS FOR STUDY:

- 1) Fundamentals of Actuarial Mathematics, Promislow, S.D(2006): John Willey, Chapters 2-11 &14.
- Newton L. Bowers, Jr, Hans U. Gerber, James C. Hickmann, Donald A. Jones and Cecil J. Nesbitt (1997): Actuarial Mathematics, The Society of Actuaries.
- 3) Compound Interest and Annuities certain by D.W.A. Donald, Heinemann, London.
- An Introduction to Mathematics of Finance, Butter Worth & Heinemann by J. J. McCutcheon and W.F.Scott.
- 5) Gnana Deep Study Maeraials.

BOOKS FOR REFERENCES:

- Actuarial mathematics by N.L. Bowers, H.U. Gerber, J.C. Hickman, D.A. Jones and C.J. Nesbitt – Published by society of Actuaries, Ithaca, Illinois, U.S.A. Second Edition (1997) Chapters: 1,2,3,4,5,9 &10
- 2) Life Contingencies, by Spurgeon Cambridge University Press.
- 3) Life Contingencies, Heinemann. Neill, A. (1977).
- 4) An Introduction to Actuarial Studies, Atkinson and Dickson (2011): Edward Publishing.
- 5) Life Contigencies by A. Neile Published by Heineman.
- 6) Modern Actuarial Theory and Practice, Philip, M. et. al (2004): Chapman and Hall.

MAPPING O	MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES										
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7				
CO1	S	S	S	S	S	S	S				
CO2	S	S	S	S	М	L	L				
CO3	S	S	S	S	L	L	М				
CO4	S	S	М	S	М	М	L				



S 3.3 (B) (22) :: TIME SERIES ANALYSIS

Credits: 4

COURSE OBJECTIVES:

- **CO 1:** To demonstrate advanced understanding of the concepts of time series analysis and their applications.
- CO 2: To demonstrate decomposition of time series tests for trend and seasonality.
- CO 3: To understand the various methods of smoothing and analysis of time series data.
- CO 4: To understand the analysis of stationary models in time series.
- CO 5: To develop stationary and non stationary models and their diagnostic check.
- **CO 6:** To acquire scientific knowledge for forecasting and applying it to various sectors.

LEARNING OUTCOMES:

At the End of this Course Students will be able to:

- LO 1: Understand and analyze components of time series.
- LO 2: Explain time series with different structures.
- LO 3: Perform trend analysis, develop seasonal indices, analysis cyclical variations and random components.
- LO 4: Smooth the data and apply various smoothing methods for data analysis.
- LO 5: Construct time series models and analyze.
- **LO 6:** Forecast with different scientific methods and become an expert in time series analysis and applications.

UNIT-I:

Time-series as discrete parameter stochastic process. Auto covariance and autocorrelation functions and their properties. Exploratory Time Series Analysis, Tests for trend.

UNIT-II:

Exponential and Moving Average Smoothing. Holt and Winters' smoothing. Forecasting based on smoothing, Adaptive smoothing.

UNIT-III:

Detailed study of the stationary process: Moving Average (MA), Auto Regressive (AR), ARMA and AR Integrated MA (ARIMA) models.

UNIT-IV:

Box – Jenkins models. Discussion (without proof) of estimation of mean, auto covariance and autocorrelation functions under large sample theory. Choice of AR and MA periods. Estimation of ARIMA model parameters. Forecasting. Residual analysis and diagnostic checking.

UNIT-V:

Spectral analysis of weakly stationary process. Periodgram and correlogram analysis. Computations based on Fourier transform.

BOOKS FOR STUDY:

- 1) Box, G.E.P. and Jenkins, G.M. (1976): Time Series Analysis –Forecasting and Control. Holden Day, San Francisco.
- 2) Anderson, T.W. (1971): The Statistical Analysis of Time Series, Wiley, New York.
- 3) Makridakis, Wheelwright and McGee: Forecasting-Methods and Applications, John Willey and Sons.
- 4) Montgomery, D.C. and Johnson, L.A.(1977): Forecasting and Time Series Analysis, McGraw Hill.

BOOKS FOR REFERENCES:

- 1) Fuller, W.A. (1976): Introduction to Statistical Time Series, John Wiley.
- N.V. Granger, C.W.J. and Newblod (1984): Forecasting Econometric Time Series, 3rd Edition, Academic Press.
- 3) Priestley, M.B. (1981): Spectral Analysis and Time Series, Griffin, London.
- 4) Kendall, Sir Maurice and Ord, J.K. (1990): Time Series Analysis. 3rd edition Edward
- 5) Kendall, M.G. and Stuart A. (1966): The Advanced Theory of Statistics, Volume 3, Charles Griffin. London.
- 6) Bloomfield, P. (1976): Fourier Analysis of Time Series An Introduction, Wiley.
- 7) Granger, C.W.J. and Hatanka, M. (1964): Spectral Analysis of Economic Time Series, Princeton Univ. Press. New Jersey.
- 8) Koopmans, L.H.(1974): The Spectral Analysis of Time Series, Academic Press.

MAP	MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES											
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7					
CO1	S	М	S	S	М	М	М					
CO2	S	М	S	the Last	М	S	М					
CO3	S	S	S	S	М	М	М					
CO4	S	S	S	S	L	М	L					
CO5	S	М	М	L	S	L	S					
CO6	S	L	S	М	М	S	L					

<u>S 3.4 (A) (22) :: RELIABILITY – I</u>

Credits: 4

COURSE OBJECTIVES:

- **CO1:** Understand the basic concepts of reliability, hazard function, bathtub curve and its applications.
- CO2: To provide an exposure to the various lifetime failure models
- **CO3:** Comprehend the importance of reliability theory in industries
- **CO4:** Construct exponential components for system reliability involved in reliability analysis
- **CO5:** Understand the importance of redundancy techniques and stand by models
- **CO6:** Exhibit theoretical knowledge on some reliability in standard probability models using complete samples for estimating the parameter and testing validity.

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO1: To learn about the basic concepts of reliability, failure rate and hazard function etc., and analyze early failure and methods
- LO2: To estimate different types of failure distributions
- LO3: To know the concepts on system reliability with exponential components in Series, Parallel and r-out of-n systems
- LO4: To evaluate the scope and with different models of each system component in system reliability
- LO5: To predict the reliability of a component, system and of a finished product.

UNIT-I

Importance of reliability, definition of reliability and its measures, concept of failure. General provision of a reliability specification, Methods of achieving reliability, Broad functions of reliability. Bath tub curve, causes of early failure and methods to avoid them.

UNIT-II

Life distributions; reliability function, hazard rate, Common failure distributions: exponential, weibull, truncated normal, log normal - their properties and uses and Estimation of parameters and tests in these models.

UNIT-III

Series, parallel and r-out of n configurations; their block diagram, reliability graph and determination of reliability through combinatorial methods. Events space, cut set and tie set, Multistate models.

UNIT-IV

System reliability with exponential components in series, parallel and r- out of - n system. Usefulness of redundancy and improvement factor. MTTF, MTBF, Equivalents MTBF of series and parallel system. Cold and hot redundancy, reliability of stand-by system. Weakest link model, chain model, stress-strength model, non-parametric estimation of reliability.

UNIT-V

Problem of life testing, estimation of parameters and reliability in standard probability models (Exponential, Weibull, Normal) using complete samples. Probability plotting and graphical procedures for estimating the parameter and testing validity of model by some standard statistical tests.

BOOKS FOR STUDY:

- 1) Probability Distributions Used in Reliability Engineering, Andrew N.O'Connor Mohammad Modarres, Ali Mosleh; Published by the Center for Risk and Reliability
- 2) Statistical Analysis of Reliability and Life-Testing Models, Bain, L.J, Dekker, New York
- 3) Statistical Models and Methods for Lifetime Data, Lawless, J.F., Wiley, New York
- 4) Bayesian Reliability Analysis, Martz, H.E. & Weller, A., Willey New York
- 5) Statistical Theory of Reliability and Life Testing Probability Models, Barlow R.E.& Proschan, F., Holt, Rinehart and Winston, New York
- 6) Reliability and Life Testing, Sinha, S.K., Wiley Eastern Limited

BOOKS FOR REFERENCES:

- 1) Applied Life Data Analysis, Nelson, W. (1982):, John Willey
- 2) Software Engineering: Design, Reliability and Management, Shooman, M.L., McGraw-Hill, New York
- 3) Reliability in Engineering Design, Kapur, K.C. and Lamberson, L.R., John Wiley, N.York
- 4) J.V. Deshpande and Sudha G. Purohit (2005) Life time data: Statistical Models and Methods World Scientific
- 5) Introduction to Reliability Analysis, Zacks S (1992), Springer Verlag, New York
- 6) Applied Reliability 3rd Edition by Paul A. Tobias, CRC Press Taylor & Francis Group.

MAPI	PING OF I	PROGRA	M OUTCO	OMES WIT	TH COUR	SE OUTCO	MES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	S	S	L	М	М
CO2	S	S	S	S	М	L	S
CO3	S	S	S	S	М	S	S
CO4	S	S	L	S	L	S	М
CO5	S	S	L	S	S	М	L
CO6	S	S	М	S	S	L	М

<u>S 3.4 (B) (22) :: BIOSTATISTICS</u>

Credits: 4

COURSE OBJECTIVES:

- **CO1:** Able to understand different statistical methods in clinical trials and their applications.
- CO2: Demonstrate different types of statistical designs and perform randomization.
- **CO3:** Summarize the biological assays such as parallel-line assay, slope-ratio assay and quantile-responses assay.
- **CO4:** Able to carry out the Categorical Data Analysis, Logistic Regression Analysis and Poison Regression Analysis and their applications.
- **CO5:** Able to measure the ANOVA for one way and two way classified data.

LEARNING OUTCOMES:

At the End of this Course Students will be able to:

- LO1: Familiarize with clinical trials and its phases I, II, III and IV.
- **LO2:** Students learn how to conduct analysis such as categorical analysis, ROC curve analysis and biological assays.
- **LO3:** Students gain knowledge about various types of regression techniques used to apply medical data especially for count data.
- LO4: Students can perform repeated measures for ANOVA one way and two way classified data.
- LO5: Students can infer about disease frequency, incidence, prevalence and relative risk.

UNIT-I:

Statistical Methods in Clinical Trials: Introduction to clinical trial and it's phases I, II, III and IV, statistical designs-fixed sample trials: simple randomized design, stratified randomized crossover design; Sequential design - open and close sequential design. Randomization Dynamic randomization, Permuted block randomization; Blinding-Single, double and triple.

UNIT-II:

Biological Assays: Introduction, parallel-line assay, slope- ratio assays and quantile- response assay, Feller's theorem. Dose-response relationships-qualitative and quantitative response, dose response relation- estimation of median effective dose – PK-PD Analysis.

UNIT-III:

Categorical Data Analysis: Categorical response data, logistic regression-odds ratio, Wald's statistic, logistic regression and its diagnostics, - Poisson regression – Estimation of relative risk and its applications.

UNIT-IV:

ROC Curve analysis - Estimation of Binomial Model and the Area under the Curve, its applications – Properties of ROC curve - Kullback –Leibler Divergence (KLD)– definition – functional relationship between Kullback –Leibler Divergence and the slope of the ROC curve – derivations of KLD expressions for Bi-normal ROC model.

UNIT-V:

Repeated Measures ANOVA – One Way and Two Classified Data –Measures of disease frequency – incidence – prevalence – relative risk – Epidemiological study designs – Cohort study design and its analysis – Case control study design and its analysis – concept of bias – information bias and selection bias.

BOOKS FOR STUDY:

- 1) Elisa T. Lee and John Wenyu Wang (2003): Statistical Methods for Survival Data analysis, 3rd edition, John Wiley.
- 2) Jerrold H. Zar (1999): Biostatistician Analysis, 4thedition, Pearson.
- 3) Armitage, P, Berry G and Mathews J.N.S (2002): Statistical Methods in Medical Research, 4th edition, Blackwell Scientific Publications.
- 4) Krzanowski, W and Hand, D.J.(2009):ROC Curves for Continuous Data, Chapman and Hall.

BOOKS FOR REFERENCES:

- 1) Hosmer and Lemeshow (2000): Applied Logistic Regression, 2nd, Wiley Series.
- 2) Alan Agresti (2002): Categorical Data analysis, 2nd, John Wiley.
- Sylvia Wasserthial and Smoller, (2004): Biostatistics and Epidemiology A Primer for Health and Biomedical professionals, 3rd edition, Springer.
- 4) Rastogi, V.B. (2006): Fundamentals of Biostatistics, ANE Books, India.

MAPF	PING OF I	PROGRA	M OUTCO	OMES WI	TH COUR	SE OUTCO	OMES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	L	S	S	М	S
CO2	S	S	L	S	S	S	S
CO3	S	S	S	М	М	L	S
CO4	S	S	М	М	М	М	S
CO5	S	S	М	S	М	L	S



M.Sc. STATISTICS

SEMESTER-IV

S 4.1 (22) :: ECONOMETRICS

Credits: 4

COURSE OBJECTIVES:

CO1: To explore the students to the special subject Econometrics which consists of the construction of general linear regression models and non-linear regression models based on the given data for a given economic phenomenon using the well-known statistical tool multiple regression analysis.

CO2: To acquaint the students about multiple regression analysis including the case of simple regression analysis which involves the estimation and validation of general linear model (GLM), then making predictions with successfully validated model.

CO3: To explore the students about the diagnostics and remedies to the problems of multicollinearity, heteroscadesticity and autocorrelation which are resulting when one or some of the assumptions of the model are violated.

CO4: To acquaint the students with some popular Qualitative regression models namely logistic regression models and probit models.

CO5: To explore the students to Autoregressive and Distributed Lag models- Stock adjustment and partial adjustment models.

COURSE OUTCOMES:

After learning the course the student will be able

LO1: To carryout simple linear regression analysis of dependent variable with one independent variable which consists of the estimation of the model, validation of the model and prediction with validated model.

LO2: To carryout regression analysis with regard to some reputed non-linear regression models like semi- log, double log and reciprocal models.

LO3: To carryout multiple linear regression analysis with several independent variables if necessary including dummy variables.

LO4: To build a general linear model (GLM) in the presence of multicollenearity, heteroscadesticity and autocorrelation.

LO5: To construct and validate polynomial, logit and probit regression models based on a given appropriate data.

LO6: To estimate the Autoregressive and Distributed Lag models namely Stock adjustment and partial adjustment models.

UNIT-I

Simple Regression Analysis: What is Econometrics? Methodology of Econometrics. Simple linear model and assumptions, Least-Squares Estimators and their properties. ML estimation of the parameters. Statistical Inference and prediction with the simple regression model. Regression analysis versus Correlation analysis, Regression analysis and ANOVA. Other functional forms of regression models –Log-linear, Semilog, reciprocal and logarithmic reciprocal models.

UNIT-II

Multiple Regression Analysis: The general linear model (GLM) and assumptions of the model, ordinary least squares (OLS) and ML estimation, properties of OLS estimators (Gauss-Markov theorem). The coefficient of determination R^2 , and Adjusted R^2 or \overline{R}^2 . Inferences about regression model, problems of prediction. Linear restrictions-- restricted least squares.

UNIT-III

Testing the structural change in regression models, Chow test for testing the equality of two regression equations. The use of dummy variables in multiple regression. The problem of multicollenearity - nature, sources, consequences, diagnostics (variance inflation factors and condition index) and remedies (Ridge regression and principle component regression methods). Aitken's generalized least squares(GLS) method.

UNIT-IV

The problem of heteroscadesticity— nature, sources, consequences, detection (Glejser Test, Goldfeld-Quandt test, Breusch-Godfrey Test, Breusch-Pagan-Godfrey Test, White's test) and remedies. The problem of auto correlation— nature, sources, consequences, detection (Durbin-Watson d-test and Breusch-Godfrey (LM) Test,) and remedies (Cochrane-Orcutt iterative procedure, C-O two-step and D-W two-step methods).

UNIT-V

Special Topics: Non-Linear Regression Models, Polynomial regression models, Qualitative Response Regression Models-The LOGIT (Logistic regression) and the PROBIT models. Errors in Variables, Instrumental Variables, Autoregressive and Distributed Lag models-Koyak, Stock adjustment and partial adjustment models.

BOOKS FOR STUDY:

- Gujarathi, D.N., Porter, D.C. and Gunasekar, S. (2011): *Basic Econometrics*, 5th Edition, McGraw Hill
- 2) Johnston, J. and DiNardo, J.(1997). *Econometric Methods*, 4th Ed., McGraw Hill
- Montgomery, D.C., Peck, E.A. and Geoffrey Vininig, G. (2003). Introduction to Linear Regression Analysis, 3rd Ed., Wiley
- 4) Koutsoyiannis, A (1979): Theory of Econometrics, Macmillan Press
- 5) Theil. H (1982): *Introduction to the Theory and Practice of Econometrics*, John Wiley.

BOOKS FOR REFERENCES:

- 1) Apte P.G. (1990): Textbook of Econometrics. Tate McGraw Hill
- 2) Intrilligator, M.D. (1980): *Econometric models Techniques and Applications*, Prentice Hall of India.
- 3) Klein, L.R.(1962): An introduction to Econometrics, Prentice Hall of India
- 4) Mai Invaud, E (1966): Statistical Methods of Econometrics, North Holland.

MAP	PING OF I	PROGRA	M OUTCO	OMES WIT	TH COUR	SE OUTCO	MES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	М	S	М	S	S
CO2	S	S	М	S	М	М	S
CO3	S	S	М	S	L	L	S
CO4	S	S	S	S	S	М	М
CO5	S	S	S	S	L	S	S



S 4.2 (22) :: ACCEPTANCE SAMPLING PLANS

Credits: 4

COURSE OUTCOMES:

- CO1: Apply acceptance and continuous sampling plan in production process.
- CO2: Able to construct sampling inspection plans for attributes and variables.
- CO3: Able to learn some advanced control charts and capability indices.
- CO4: Able to construct Six Sigma limits.

LEARNING OUTCOMES:

- LO1: Acquainted with Six Sigma and lean thinking in industrial experimentation.
- LO2: Can identify the cause of defects using statistical quality management techniques.
- LO3: Able to apply statistical quality control techniques to minimize the variability in manufacturing and business process.

UNIT – I:

Attribute Sampling Plans: Introduction, advantages and disadvantages of sampling, Producer's risk and Consumer's risk, Operating Characteristic curve, evaluating sampling plans using average out going quality limit, average sample number. Lot-by-Lot attribute sampling plans: Single sampling plans – The OC curve, design of single sampling plans, double sampling plans, The OC curve , ASN curve, design of double sampling plan sequential sampling plan, standard sampling plans-Military Standard 105E and Dodge – Roming sampling plan.

UNIT – II:

Acceptance sampling plans for variables, Introduction, advantages and disadvantages of sampling, variable sampling plans for a process parameter – Estimating process average – Single specification limit and known process standard deviation, estimating process average – double specification limits and known process standard deviation, estimating process average – Single specification limit and unknown process standard deviation. Standardized plans – MIL-STD-414, Sequential sampling plan by variables.

UNIT – III:

Acceptance sampling procedures – importance, procedures, advantages and disadvantages of Chain sampling plan, Skip-lot sampling plan, Continuous sampling – CSP-1, CSP-2, CSP-3 and multi-level plans, Military standard sampling plan –MIL STD 1235b.

UNIT – IV:

Industrial Experimentation, Fractional factorial experiments, Response surface methodology, Six sigma in process improvement and product development. Wald-Wolfwitz type and their properties.

$\mathbf{UNIT} - \mathbf{V}$:

Rectifying inspection by Lot-By-Lot Sampling: Rectifying Inspection Plans Calling for 100 Percent inspection of Rejected Lots. Rectifying Inspection Plans with less than 100 Percent inspection of Rejected Lots.

BOOKS FOR STUDY:

- 1) Introduction to Statistical Quality Control, Montgomery, D.C., John Wiley (Asia) 2001.
- 2) Modern Methods for Quality Improvement, H.M.Wadsworth, K.S.Stephens A.B.Godftrey, Second Edition; 2004, John Wiley and sons.
- 3) The Essence of TQM, John Bank, Printice, Hall of India Pvt Ltd (1998).
- 4) Statistics of Quality Control Sampling Inspection and Reliability by S.Biswas, New central book agency Pvt Ltd (2003).

BOOKS FOR REFERENCES:

1) R.C. Guptha (2001): Statistical Quality Control. 9th Edition. Khanna Publishers.

- 2) Duncan Acheson (1986): Quality Control and Industrial Statistics. 5th Edition. Irvin.
- Statistical Quality Control 7th edition, E.L. Grant & R.S. Leavenworth; McGraw Hill, New York.

MAP	PING OF	PROGRA	M OUTC	OMES WI	TH COUR	SE OUTC	OMES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	M	S	М	S	S
CO2	S	S	S	S	M	S	S
CO3	S	М	S	S	L	L	S
CO4	S	S	М	Sec. Sec. St	M	L	M

S 4.3 (A) (22) :: OPERATIONS RESEARCH

Credits: 4

COURSE OBJECTIVES:

- CO1: To acquire knowledge of scope of Operations Research
- CO2: Understand to develop the optimization techniques that will be useful in the personal and professional life
- CO3: Can apply Game theory to analyze existing situations wherever there are limited resources, different decision options and different outcomes from different choices.
- CO4: To find optimum solution and formulate LPP to solve problems using simplex methods
- CO5: To apply with inventories of various goods with and without shortages to solve real life problems and derive study state solutions of Poisson queues
- CO6: Using PERT and CPM able to find the minimum time required to complete project when it involves interdependent activities.

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO1: To Formulate the problem in operations research.
- LO2: To Establish the relationship between the variables and constraints by constructing the model to analyze existing situations wherever there are limited resources, different decision options, different outcomes from different choices.
- LO3: To provide the idea of formulating mathematical model and their optimum solution in the contest of practical problems belonging to Government /Private sectors.
- LO4: To Learn the tools like Linear Programming Problems, replacement and operational gamming.
- LO5: To Familiar with the queuing and different design and develop inventory models
- LO6: To Obtain a firm foundation in advanced OR techniques for the real life problems.

UNIT-I:

Games as decision problems, Two-person Zero-Sum game, Pure and mixed Strategies, maximum criterion, dominance, minimax theorem. Solutions of 2X2, 2Xm, nX2 games and 3X3 games (using simplex algorithm).

UNIT-II:

Inventory control, models of inventory-purchase model with instantaneous replenishment and without shortages, Manufacturing model without shortages, Purchase model with instantaneous Replenishment and with shortages. Manufacturing model with shortages, Operation of inventory system, Quantity Discount - Price breaks - Purchase Inventory Model with one price break, two price breaks and any number of price breaks.

UNIT-III:

Queueing models - Characteristics of Queueing Systems, Classification of Queues. Steady-state solution of $M/M/1/\infty/FCFS$, M/M/1/N/FCFS, $M/E_k/1$ models and M/G/1 queue - length Pollazek - Khinchine result.

UNIT-IV:

Replacement and maintenance analysis-Types of maintenance, Types of replacement problems, Determination of economic life of an asset, Basics of interest formulae – Present-worth factor (P/F, i, n), Equal payment series capital recovery factor (A/P, i, n). Simple probabilistic model for items which completely fail.

UNIT-V:

Project management; CPM and PERT; probability of project completion, crashing.

BOOKS FOR STUDY:

- 1) Hillier, F.S. and Leiberman(2017)G.J., Holden Dev, Introduction to Operations Research.
- 2) Sharma, J.K., 2003, Operations Research Theory and Applications, Macmillan, India
- 3) Kantiswarup, Gupta, P.G. and Man Mohan, Operations Research, Sultan Chand & Sons
- 4) S.D. Sharma, Operations Research, Kedar Nath Ram Nath & Co, Meerut
- 5) Panneerselvam. R, Operations Research, Printice Hall of India, Pvt Ltd.
- 6) Churchman, C.W., Ackoff, R.L. and Amoff, E.L. (1957). Introduction to Operations Research.

BOOKS FOR REFERENCES:

- 1) Philps D.T. Ravindran A and Sal berg J., Operations Research, Principles and practice, John Wiley
- 2) Donald Gross and Carl M.Harrsis, Fundamentals of Queueing Theory, John Wiely
- 3) Leonard Kleinrock, Queueing System, volume 1. Wiley Inter science
- 4) Taha, HA. (1982). Operational Research
- 5) Philips, D.T., Ravindran, A. and Solberg, J. Operations Research, Principles and Practice

MAP	MAPPING OF PROGRAM OUTCOMES WITH COURSE OUTCOMES											
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7					
CO1	S	S	М	S	S	S	М					
CO2	S	S	S	S	S	L	L					
CO3	S	S	S	S	М	S	L					
CO4	S	S	М	S	М	S	S					
CO5	S	S	L	М	L	М	L					
CO6	S	S	М	S	S	М	S					

S 4.3 (B) (22) :: MACHINE LEARNING USING PYTHON

Credits: 4

COURSE OBJECTIVES:

- CO 1: Comfortably Perform basics operations in Python
- CO 2: Understand machine learning concepts
- CO 3: Explore and execute the machine learning concepts for real time data using Python

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO 1: Perform basic operations and concepts in Python
- LO 2: Understand and use the essential modules in Python
- LO 3: Evaluate the scope and opportunities of machine learning
- LO 4: Gain knowledge and hands-on training in machine learning techniques
- LO 5: explore program skills for machine learning techniques

UNIT-I

Type of variables, data types, lists, control statements, functions, classes, files and exceptions.

UNIT-II

Jupyter Notebook, Numpy, Scipy, Matplotlib, Pandas, mglearn.

UNIT-III

Classification and Regression, k-Nearest Neighbors, Decision Trees, Neural Networks.

UNIT-IV

Preprocessing and Scaling, Scaling training, Dimensionality Reduction, Feature

Extraction, and Manifold Learning.

UNIT-V

Clustering: k- Means clustering, Agglomerative Clustering, DBSCAN.

BOOKS FOR STUDY:

- Introduction to Machine Learning with Python A Guide for Data Scientists by Andreas C. Muller & Sarah Guido(2017), O'Reilly
- 2) Machine Learning in Python: Essential Techniques for Predictive Analysis by Micheal Bowles (2015), Wiley
- 3) Python Crash Course: A hands-on, Project-Based Introduction to Programming by Eric Matthes (2016), no starch press.

BOOKS FOR REFERENCES:

- Python for Probability, Statistics and Machine Learning (second edition) (2019) by Jose Unpingco, Springer
- 2) Practical Statistics for Data Scientists(second edition)(2020) by Peter Bruce, Andrew Bruce & Peter Gedeck, O'Reilly.

MAP	PING OF	PROGRA	M OUTCO	OMES WIT	TH COUR	SE OUTCO	MES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	S	S	М	М	S
CO2	S	S	L	S	S	М	S
CO3	S	М	S	S	L	L	S



<u>S 4.4 (A) (22) :: RELIABILITY – II</u>

Credits: 4

COURSE OBJECTIVES:

- CO1: Understand the basic concepts of Repairable and Non-Repairable systems and its applications
- CO2: Know the concepts bounds on system reliability; structural and reliability importance of components
- CO3: Learn reliability theory and analysis of survival data
- CO4: Familiar with different concepts of reliability and lifetime models
- CO5: Understand the special kinds of various Fault Trees construction used in reliability
- CO6: To evaluate the concepts of IFR, IFRA, NBU, DMRL, and NBUE.

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO1: To learn about the basic concepts of one/two components in Repairable and Non-Repairable systems reliability
- LO2: Recall to estimate the parameters of lifetime distributions
- LO3: To explain and compute the structural properties of coherent system
- LO4: To evaluate the structure function using modular decomposition
- LO5: To expertise to use fundamentals and procedures of FTA formats and FMEAs etc.,
- LO6: To familiar distinguish between the concepts of Notions of Ageing
- LO7: Get theoretical knowledge of computing probability of survival of machines, models related to production in industries and can draw conclusions.

UNIT-I:

(i) Non-Repairable System:

Single element-non repairable, two element-non-repairable system; solution through Laplace transform. Poisson process, Stand-by system.

(ii) Repairable System:

Reliability and availability function of one and two components system, up-time and downtime ratio, steady state probabilities.

UNIT-II:

Coherent System and its Structural Properties:

Systems with independent components, coherent system, path sets and cut sets, reliability of coherent system, bounds on system reliability, Relative importance of components, Modular decomposition of coherent system and improved bounds for system reliability. Concept of associated random variables.

UNIT-III:

Fault Tree Analysis:

Event tree, simple fault tree and its construction, Mathematics of FTA, Efficiency of FTA formats, FTA, Event space method, Monte-Carlo technique, Min-cut set algorithm, FMEA, Carrying out FMEA with practical example.

UNIT-IV:

Life distributions – reliability function; hazard rate; common life distributions-Exponential, Gamma, Weibull, Lognormal, Pareto. Estimation of parameters and tests in these models. Life tables, mean residual life and their elementary properties.

UNIT-V:

Notions of Ageing classes – IFR, IFRA, NBU, DMRL and NBUE and their duals. Estimation of survival function-Acturial Estimator, Kaplan–Meier Estimator, Semi– parametric regression for failure rate–Cox's proportional hazards model with one and several covariates.

BOOKS FOR STUDY:

- 1) Reliability Engineering Theory and Practice, A. Birolini, Fourth Edition, Springer Int.
- 2) Bayesian Reliability Analysis, Martz, H.E. & Weller, A., Willey New York
- 3) Reliability and Life Testing, Sinha, S.K., Wiley Eastern Limited
- 4) Probability Distributions Used in Reliability Engineering, Andrew N.O'Connor Mohammad Modarres, Ali Mosleh; Published by the Center for Risk and Reliability
- 5) Statistical Analysis of Reliability and Life-Testing Models, Bain, L.J, Dekker, New York
- 6) Statistical Models and Methods for Lifetime Data, Lawless, J.F., Wiley, New York

BOOKS FOR REFERENCES:

- 1) Statistical Theory of Reliability and Life Testing Probability Models, Barlow R.E.& Proschan, F., Holt, Rinehart and Winston, New York.
- 2) Introduction to Reliability Analysis, S. Zacks, Springer Verlag, N.Y.
- 3) Gross A.J. and Clark, V.A.(1975) Survival Distributions: Reliability Applications in the Biomedical Sciences, John Wiley and sons.
- 4) Cox, D.R. and Oakes, D. (1984) Analysis of Survival Data, Chapman and Hall, New York
- 5) Elandt-Johanson, R.E.Johnson N.L. (1980) Survival models and Data Analysis, John Wiley and Sons.
- 6) Miller, R.G. (1981) Survival Analysis (Wiley).

MAP	PING OF	PROGRA	M OUTC	OMES WI	TH COUR	SE OUTCO	OMES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	S	S	М	L	S
CO2	S	S	S	S	М	L	М
CO3	S	М	S	S	М	М	M
CO4	S	S	М	М	S	S	S
CO5	S	М	М	L	S	L	S
CO6	S	S	М	S	S	L	L



S 4.4 (B) (22) :: KNOWLEDGE DISCOVERY AND DATA MINING

Credits: 4

COURSE OBJECTIVES:

- CO1: Able to outline classification methods.
- CO2: To get expertise in different clustering methods.
- CO3: Able to learn unsupervised learning techniques.
- CO4: To acquaint with supervised learning techniques.
- CO5: Able to get familiarity with analytical data processing.

LEARNING OUTCOMES:

At the End of this Course Students will be able:

- LO1: Able to perform multivariate analysis with data sets.
- LO2: Able to infer vector quantization methods.
- LO3: Obtain a firm foundation in dimension reduction, feature selection and clustering techniques.
- LO4: To appraise regression trees in predictive modeling.
- LO5: To construct association rules on data sets.

UNIT-I:

Review of classification methods from multivariate analysis; classification and decision trees.

UNIT-II:

Clustering methods from both statistical and data mining viewpoints; vector quantization.

UNIT-III:

Unsupervised learning from univariate and multivariate data; dimension reduction and feature selection.

UNIT-IV:

Supervised learning from moderate to high dimensional input spaces; regression trees.

UNIT-V:

Introduction to databases, including simple relational databases; data warehouses and introduction to online analytical data processing. Association rules and prediction; data attributes.

BOOKS FOR STUDY:

- 1) A. Berson and S.J. Smith (1997): Data Warehousing, Data Mining and OLAP. McGraw-Hill.
- 2) L.Breiman, J.H. Friedman, R.A. Olshen, and C.J.Stone (1984): Classification Regression Trees. Taylor Francis.

- J.Han and M. Kamber (2006): Data Mining; Concepts and Techniques. 2nd Edition. Morgan Kaufmann.
- 4) T.M. Mitchell (2011): Machine Learning. Springer

BOOKS FOR REFERENCE:

1) B.D.Ripley (2008): Pattern Recognition and Neural Networks. Cambridge University Press.

MAP	PING OF 1	PROGRA	M OUTCO	OMES WIT	TH COUR	SE OUTC	OMES
COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7
CO1	S	S	L	S	S	S	S
CO2	S	S	S	S	S	S	S
CO3	S	S	L	S	М	S	S
CO4	S	S	М	S	М	М	S
CO5	S	S	S	S	L	S	S

